

*Seminář Hvězdárny Valašské Meziříčí*

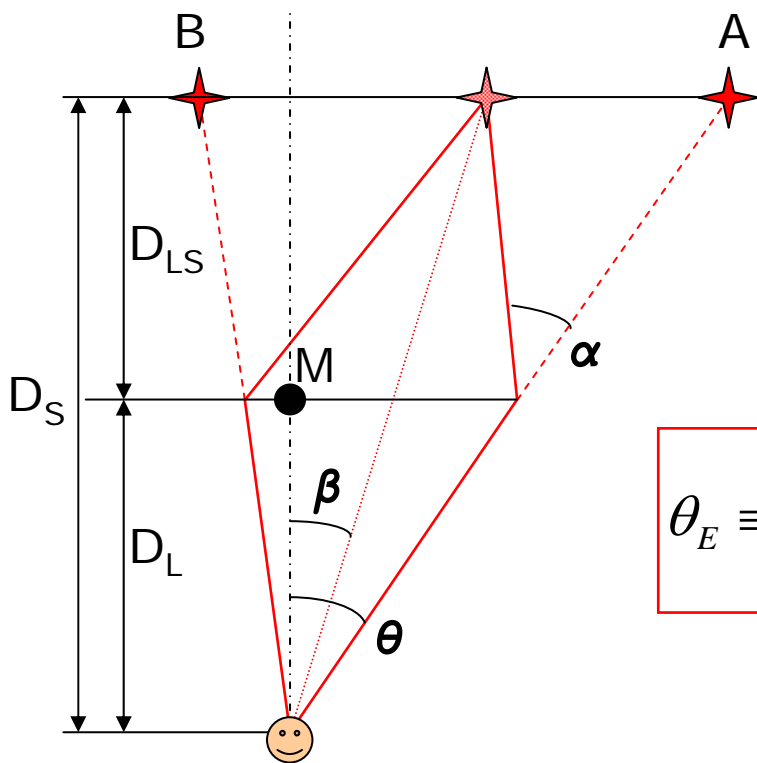
*24.10.2009*

# **Detekce planet gravitačním mikročočkováním**

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# Gravitační čočka



čočková rovnice

$$\beta = \theta - \frac{D_{LS}}{D_S} \alpha(\theta)$$

jednoduchá čočka:  $\alpha(\theta) = \frac{4GM}{c^2 D_L \theta}$

$$\theta_E \equiv \sqrt{\frac{4GM D_{LS}}{c^2 D_L D_S}}$$

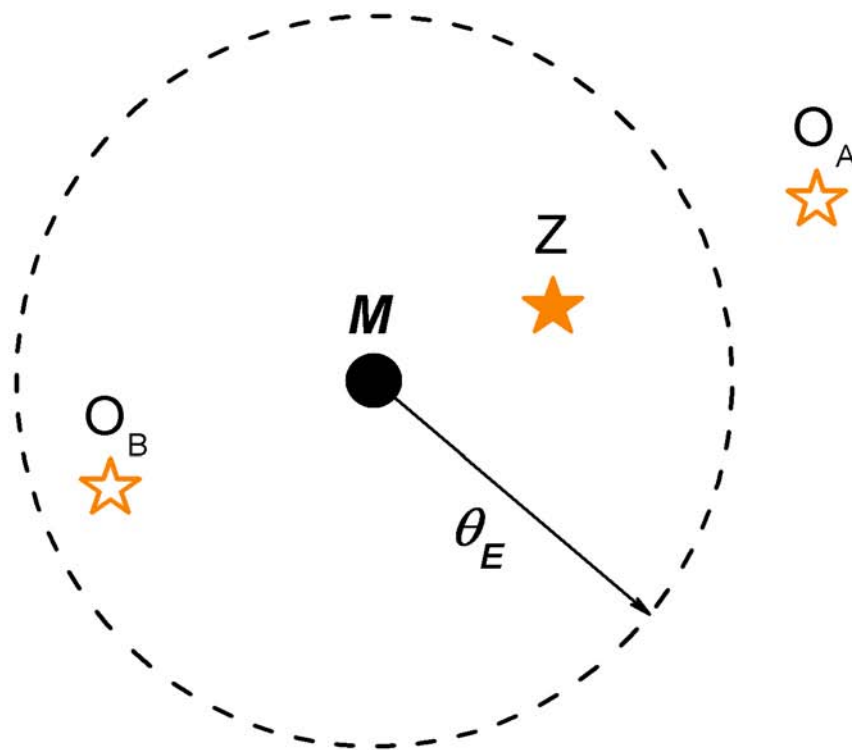
Einsteinův poloměr

poloha obrazů pro

$$\beta = 0 \dots |\theta| = \theta_E$$

$$\beta \neq 0 \dots \theta_{A,B} = \left( \frac{1}{2} \pm \sqrt{\frac{1}{4} + \frac{\theta_E^2}{\beta^2}} \right) \beta$$

viděno na nebi



# Režimy gravitačního čočkování

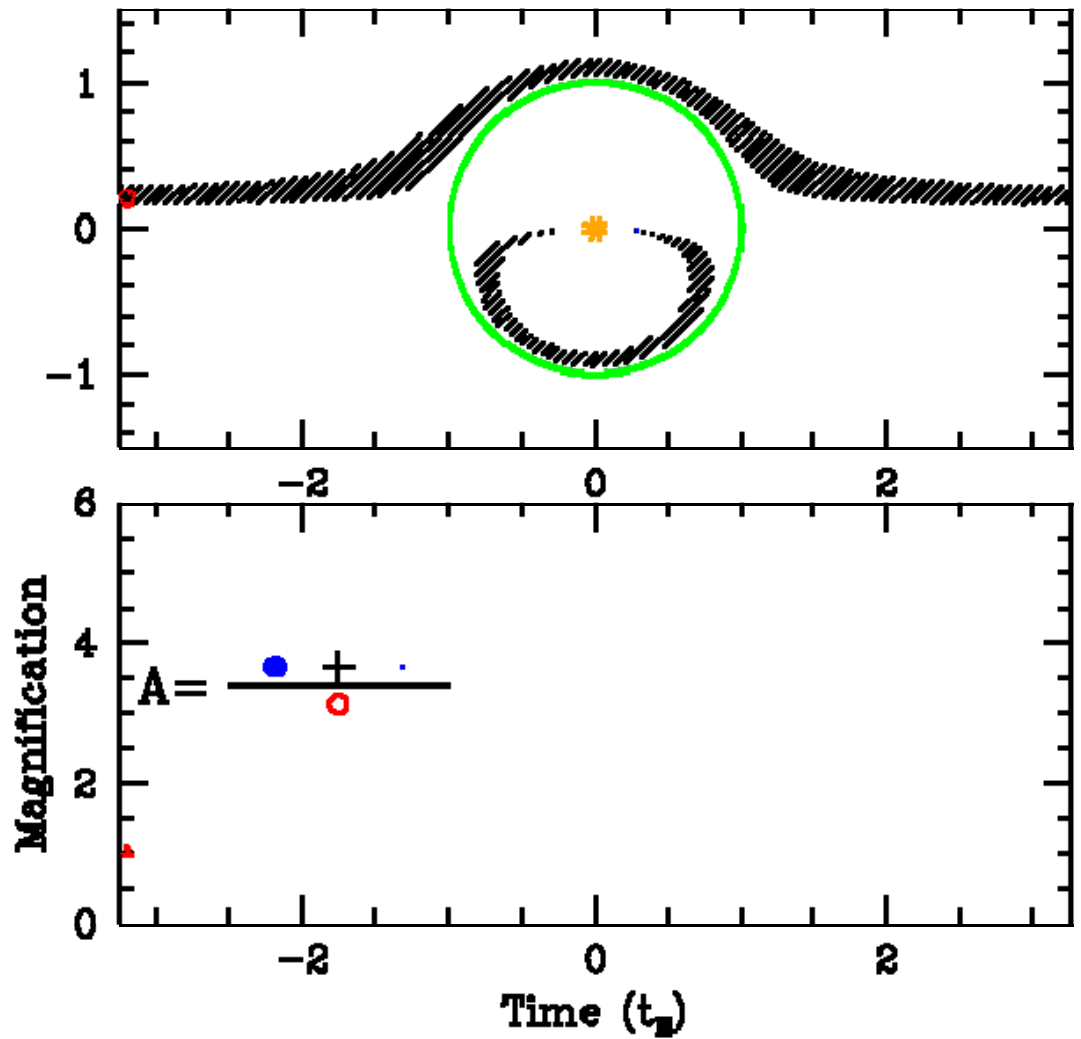
**silné čočkování** – pozorování násobných obrazů zdroje  
(Č: galaxie, kupa galaxií; Z: kvasar, galaxie)

**slabé čočkování** – měření deformace hlavního obrazu zdroje  
(Č : kupa galaxií, větší struktury; Z: galaxie)

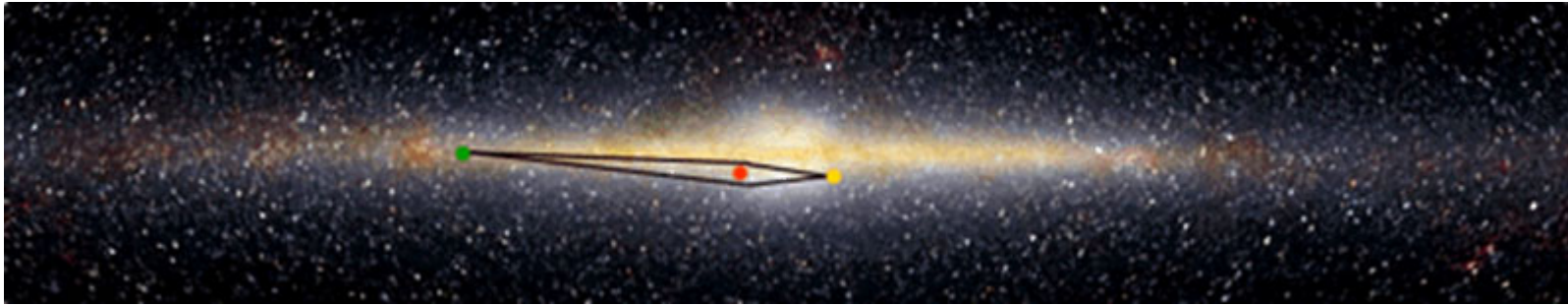
**mikročočkování** – pozorování časově proměnného zjasnění  
(Č : hvězda, hvězdná soustava; Z: hvězda, kvasar)

# Zjasnění světelného toku

$$A_0(\beta) = \frac{\beta^2 + 2\theta_E^2}{|\beta| \sqrt{\beta^2 + 4\theta_E^2}}$$

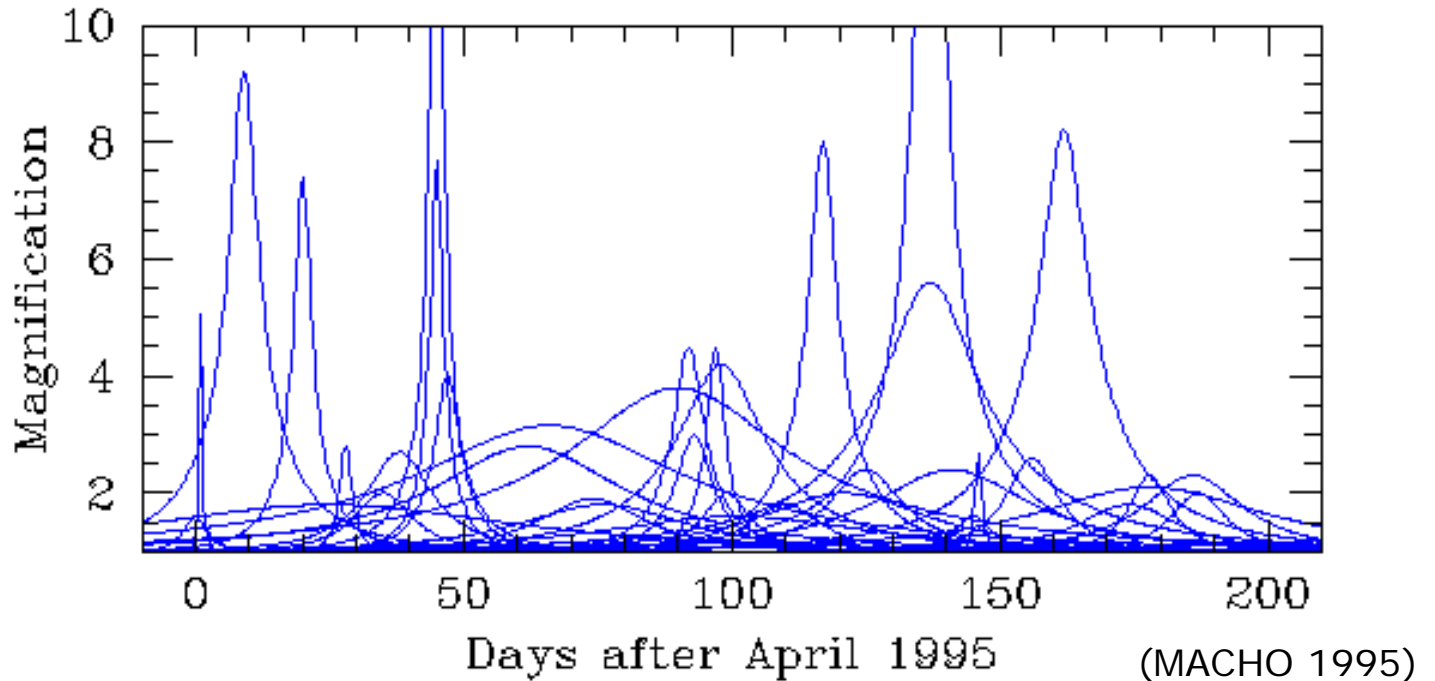


## Pozorování: monitorovací projekty (MACHO, EROS, **OGLE**, MOA)

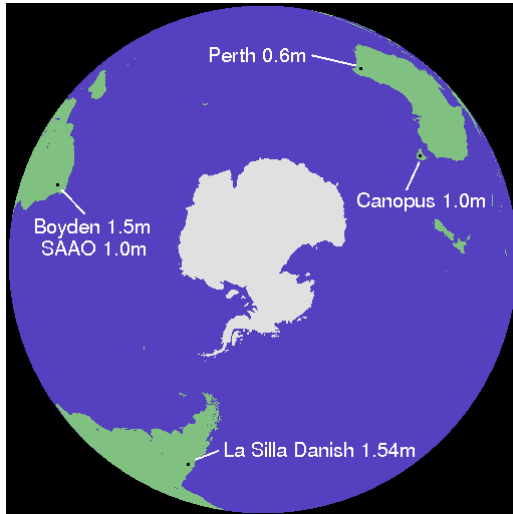


MOA

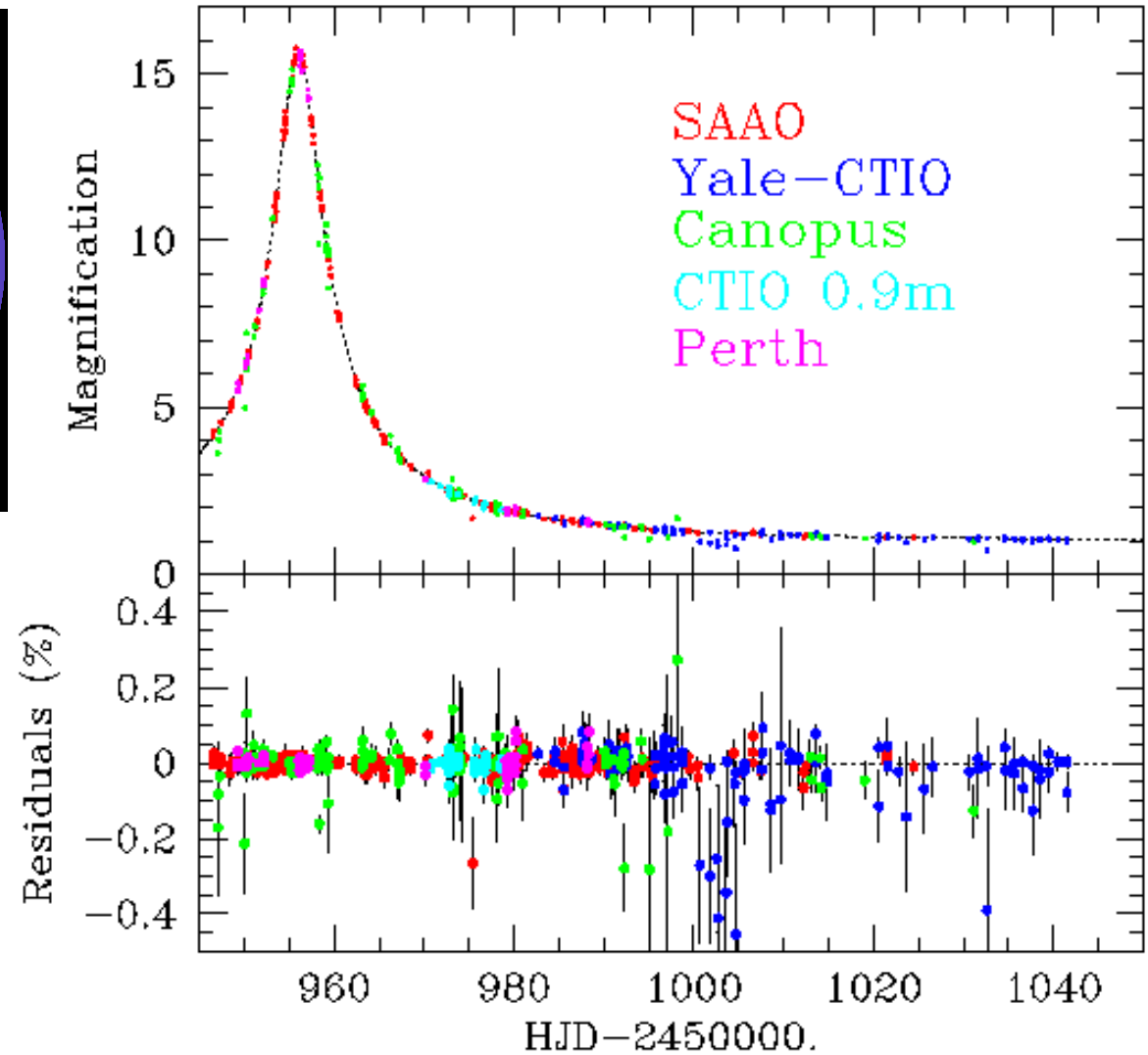
V období 1992 – III/2009 napozorováno ~ 6600 mikročoček



# Návazné projekty (PLANET, $\mu$ Fun, GMAN, MPS)



PLANET



PLANET (OGLE-1998-BUL-14)

# Dvojitá mikročočka

$$\vec{\alpha}(\vec{\theta}) = \frac{4GM}{c^2 D_L} \left[ \mu_A \frac{\vec{\theta} - \vec{\theta}_A}{|\vec{\theta} - \vec{\theta}_A|^2} + \mu_B \frac{\vec{\theta} - \vec{\theta}_B}{|\vec{\theta} - \vec{\theta}_B|^2} \right]$$

po přeškálování  $\vec{\beta} = \theta_E \vec{y}$ ,  $\vec{\theta} = \theta_E \vec{x}$

čočková rovnice:

$$\vec{y} = \vec{x} - \mu_A \frac{\vec{x} - \vec{x}_A}{|\vec{x} - \vec{x}_A|^2} - \mu_B \frac{\vec{x} - \vec{x}_B}{|\vec{x} - \vec{x}_B|^2}$$

klíčové parametry:  $q = \mu_A / \mu_B$

hmotnostní poměr

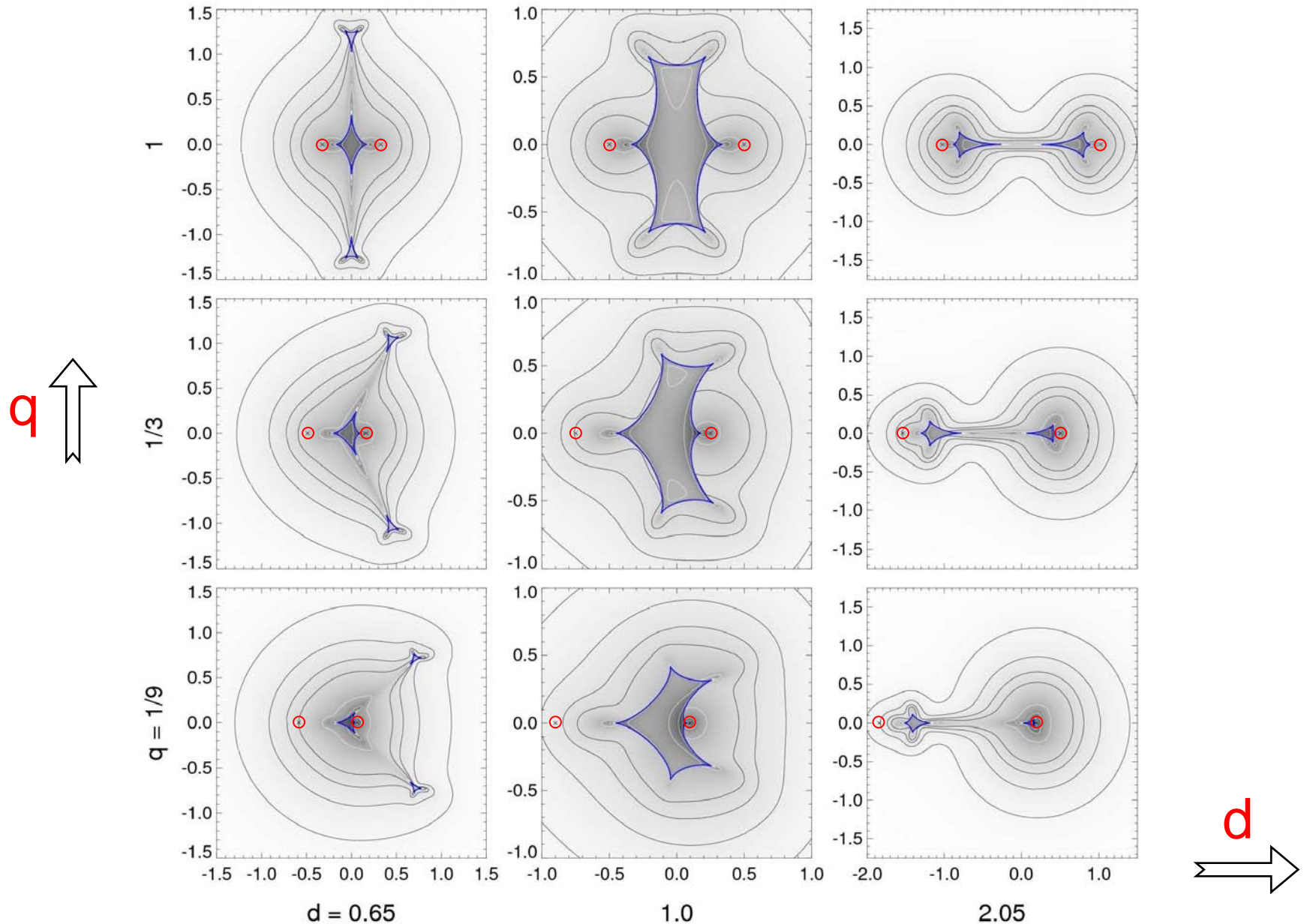
$$d = |\mathbf{x}_B - \mathbf{x}_A|$$

průmět vzáj. vzdálenosti

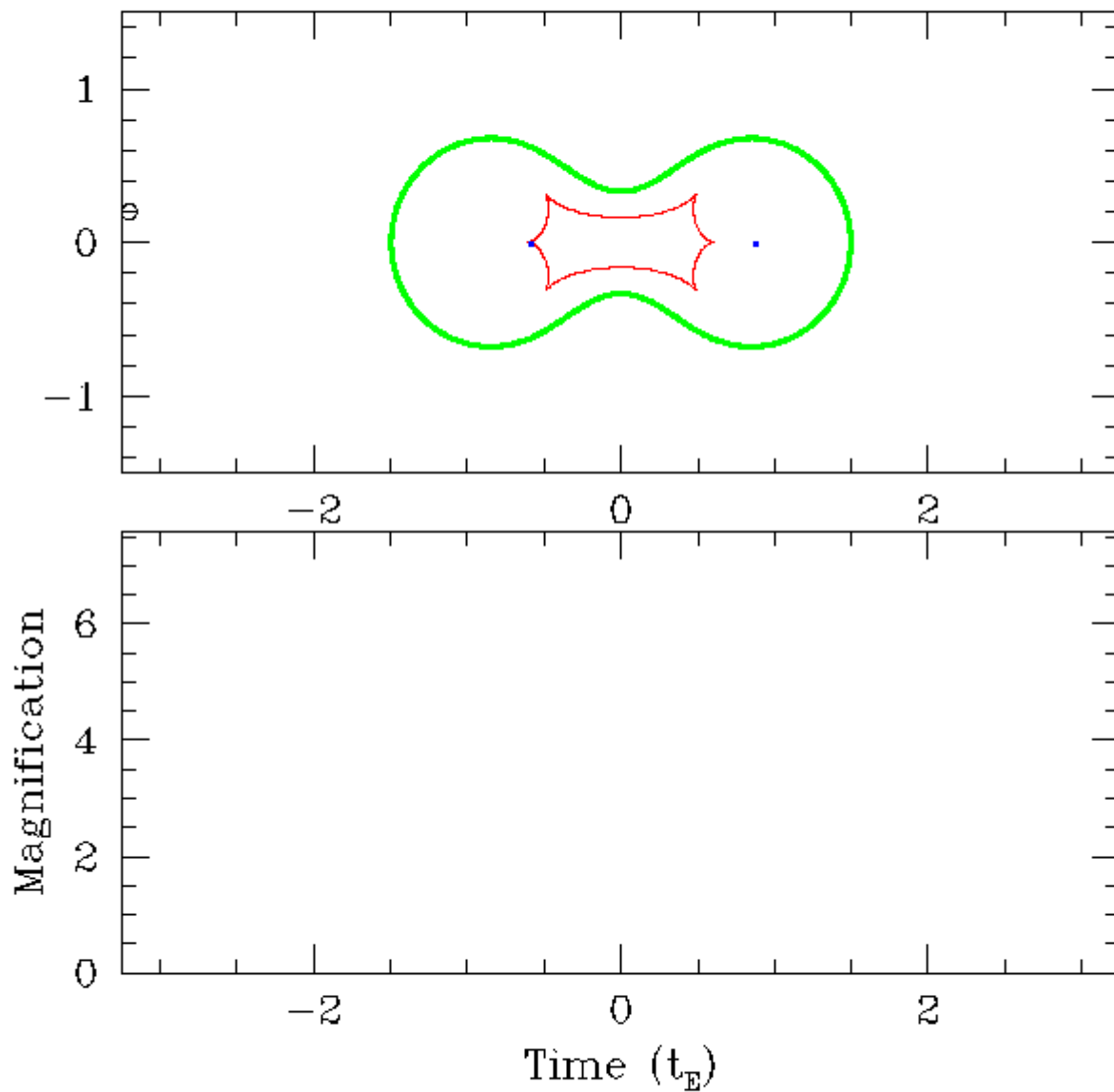
pokud  $q \ll 1$   $\Rightarrow$  **Mikročočka s planetou**



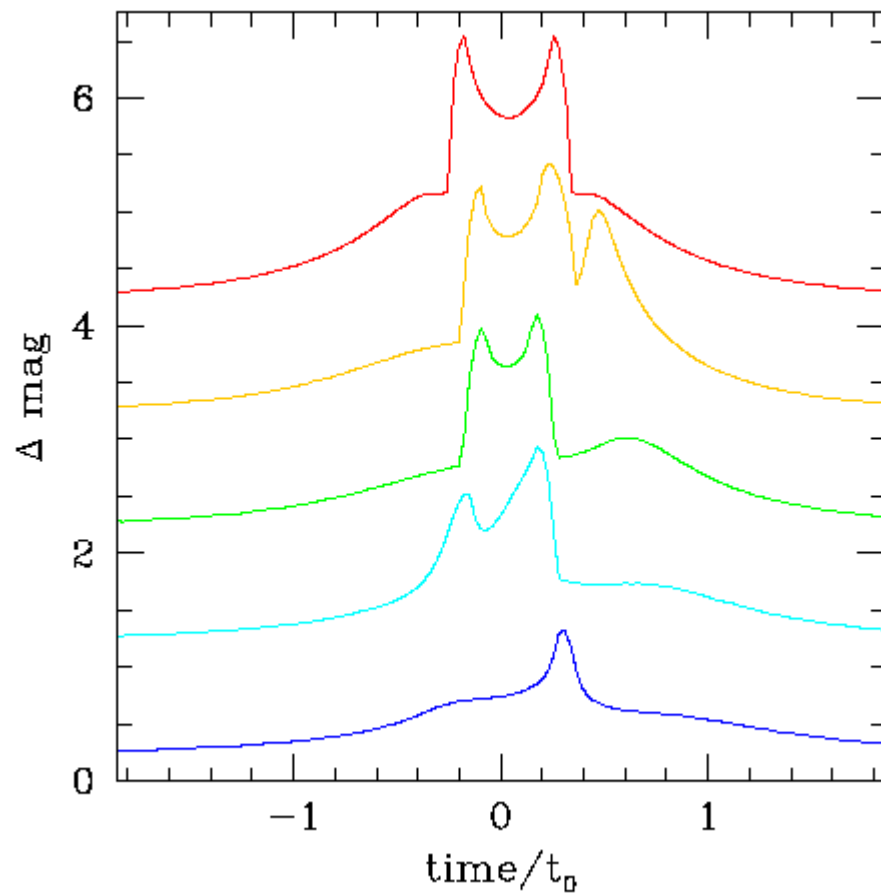
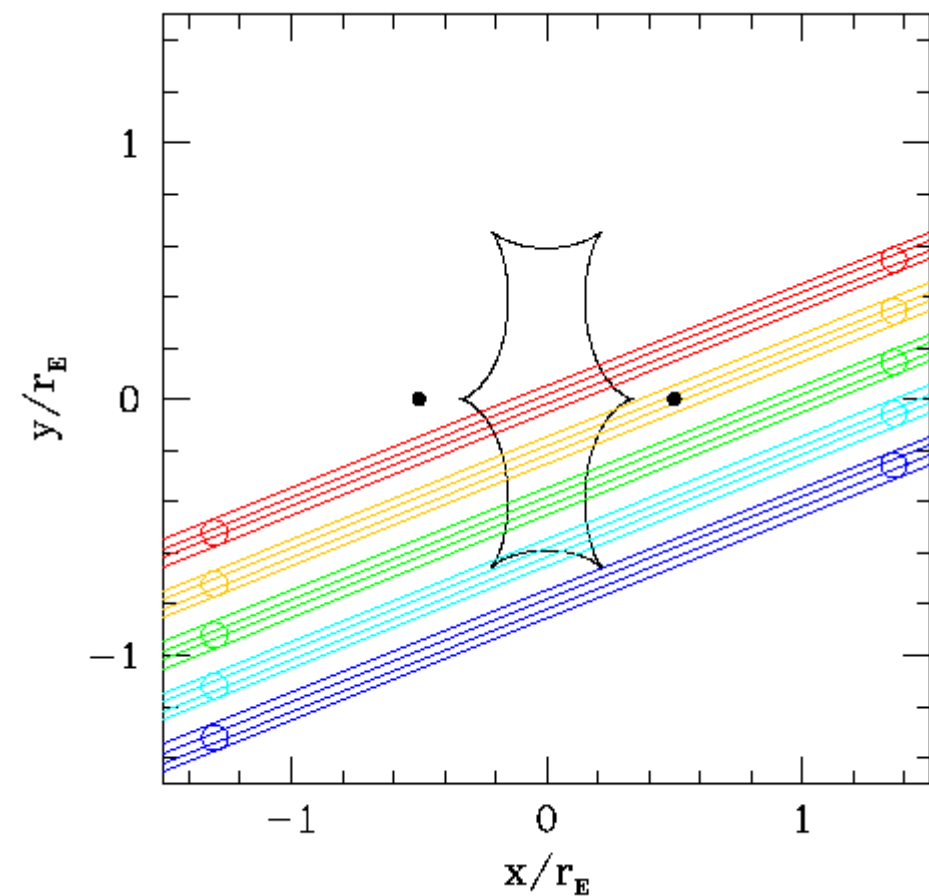
# Zjasnění bodového zdroje dvojitou mikročočkou



# Obrazy + světelná křivka

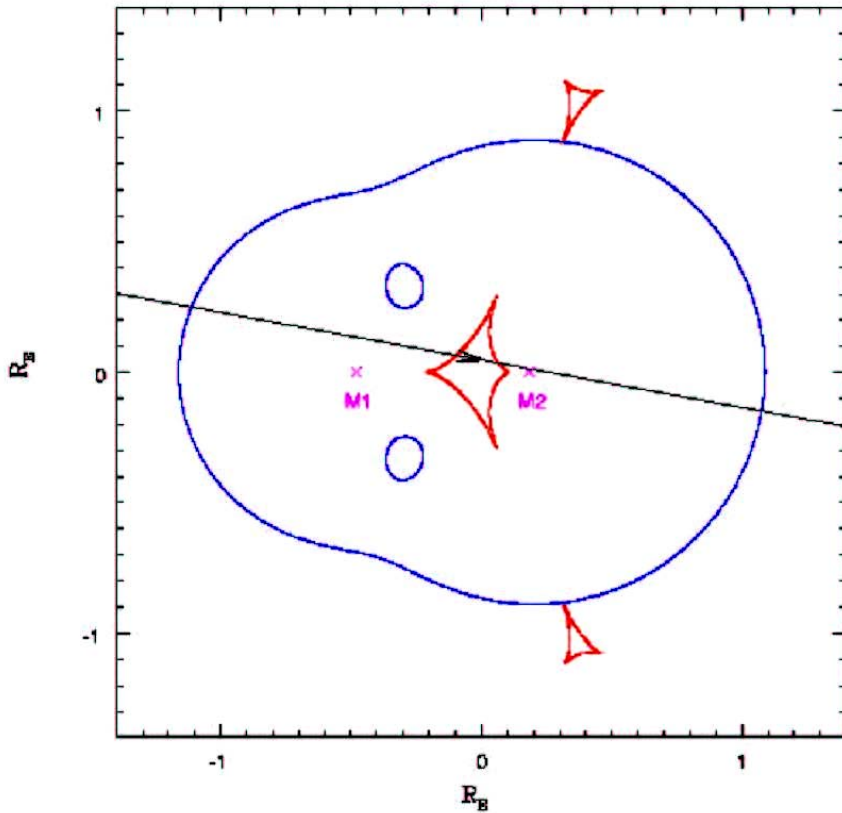


# Příklady světelných křivek

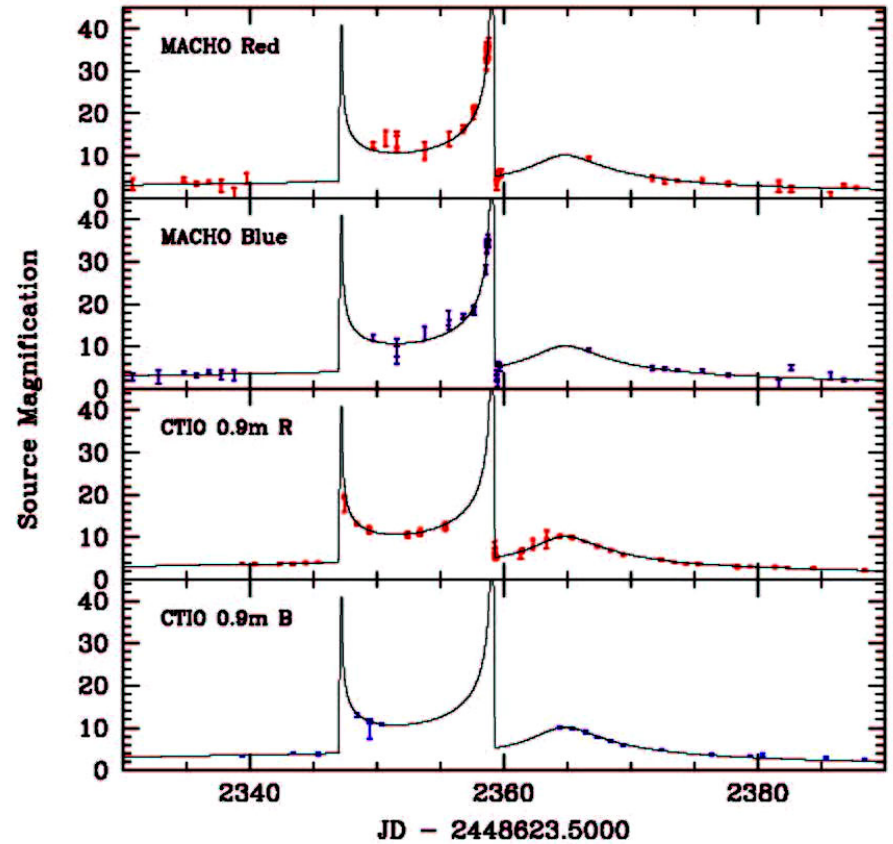


# Pozorovaná dvojitá mikročočka

MACHO Event 98-SMC-1



MACHO Event 98-SMC-1



# Detekce planet u mikročoček

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## OGLE 2003-BLG-235/MOA 2003-BLG-53: A PLANETARY MICROLENSING EVENT

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THE MOA AND OGLE COLLABORATIONS

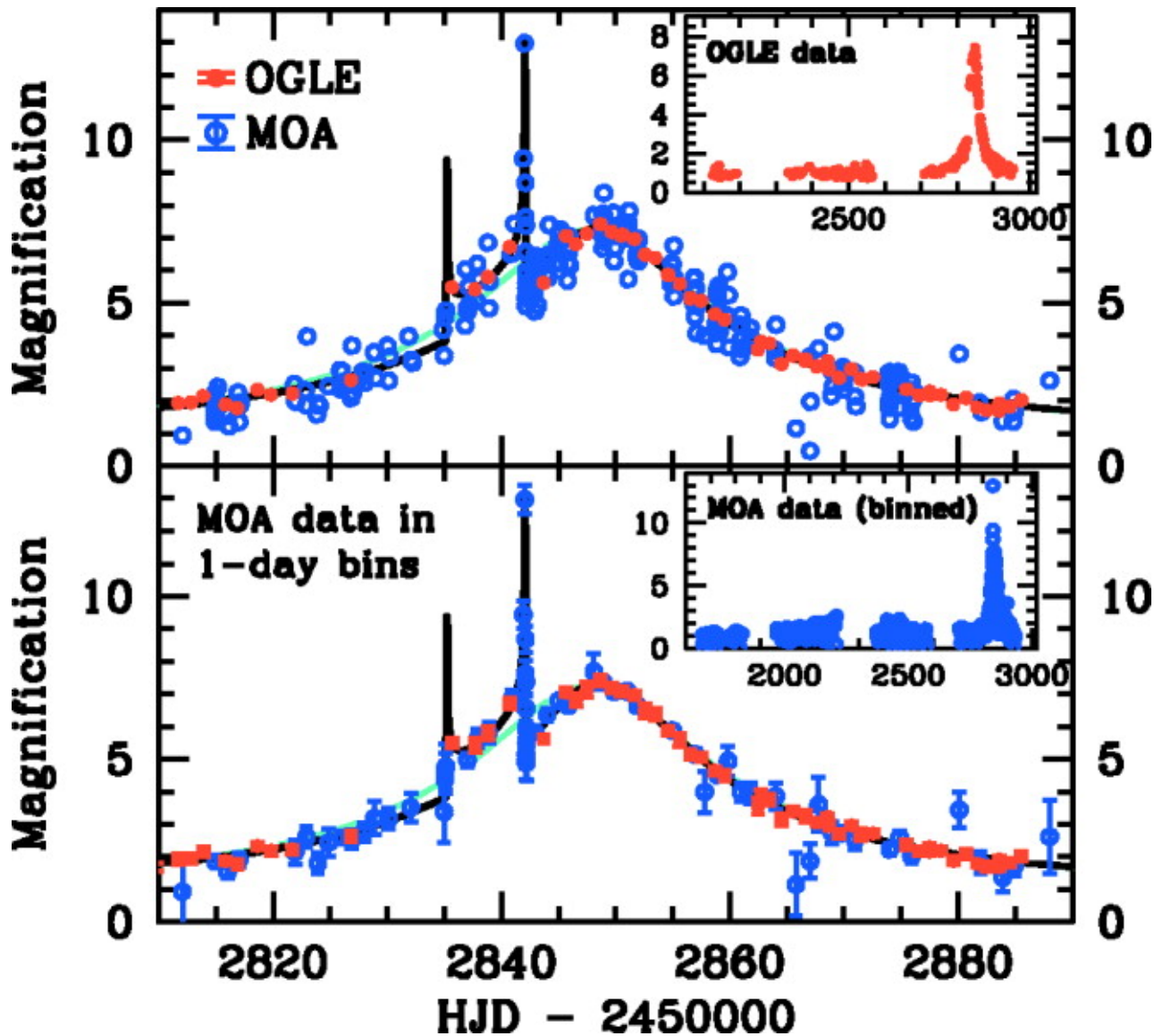
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### ABSTRACT

We present observations of the unusual microlensing event OGLE 2003-BLG-235/MOA 2003-BLG-53. In this event, a short-duration ( $\sim 7$  days) low-amplitude deviation in the light curve due to a single-lens profile was observed in both the MOA (Microlensing Observations in Astrophysics) and OGLE (Optical Gravitational Lensing Experiment) survey observations. We find that the observed features of the light curve can only be reproduced using a binary microlensing model with an extreme (planetary) mass ratio of  $0.0039^{+11}_{-07}$  for the lensing system. If the lens system comprises a main-sequence primary, we infer that the secondary is a planet of about 1.5 Jupiter masses with an orbital radius of  $\sim 3$  AU.

# OGLE 2003-BLG-235 / MOA 2003-BLG-53

Bond et al. (2004)



$$q = 0,0039^{+0,0011}_{-0,0007}$$

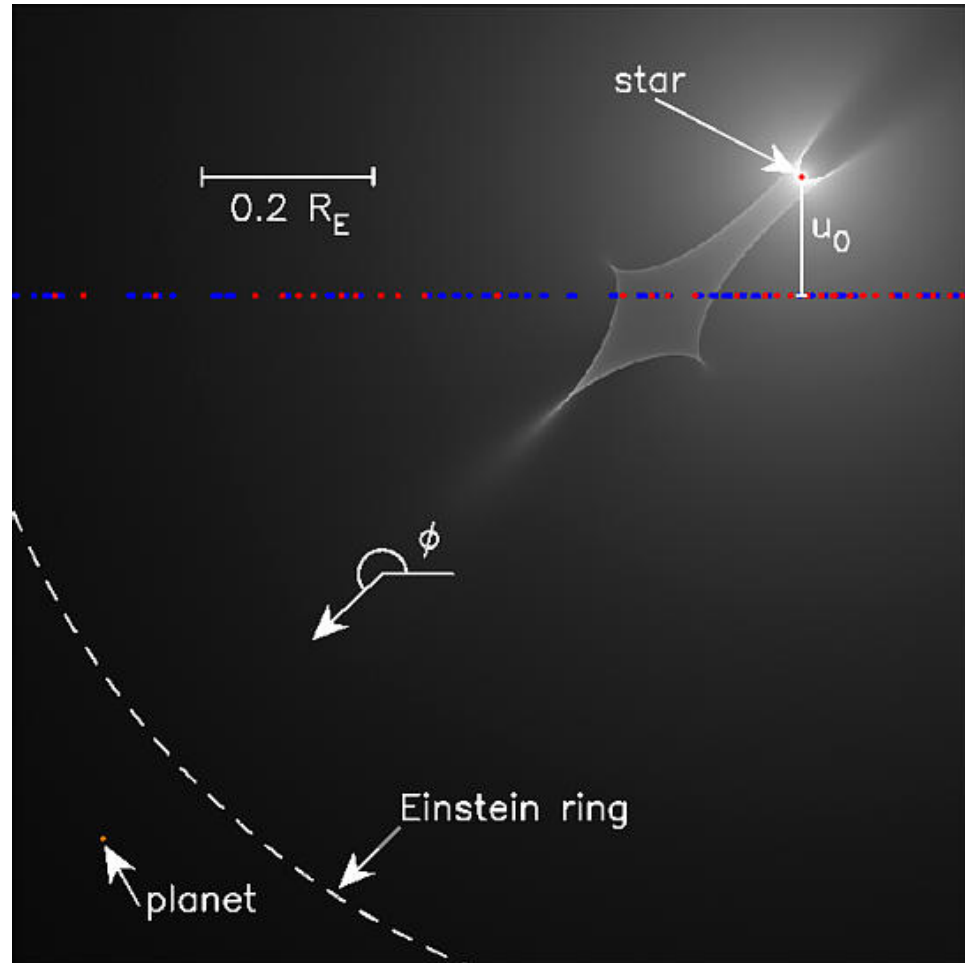
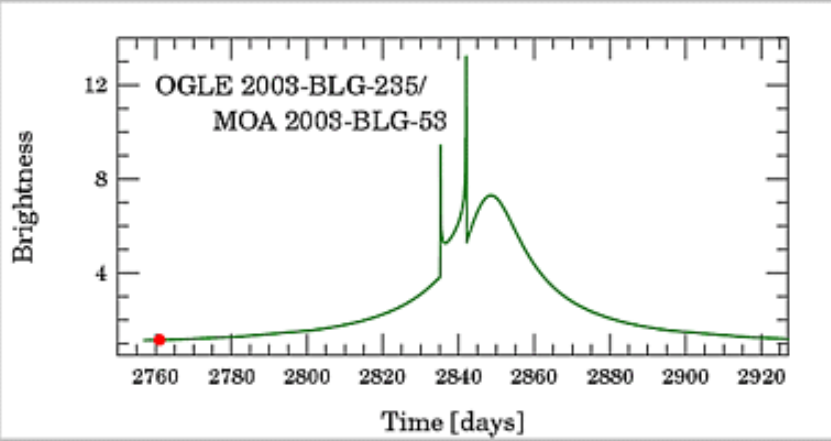
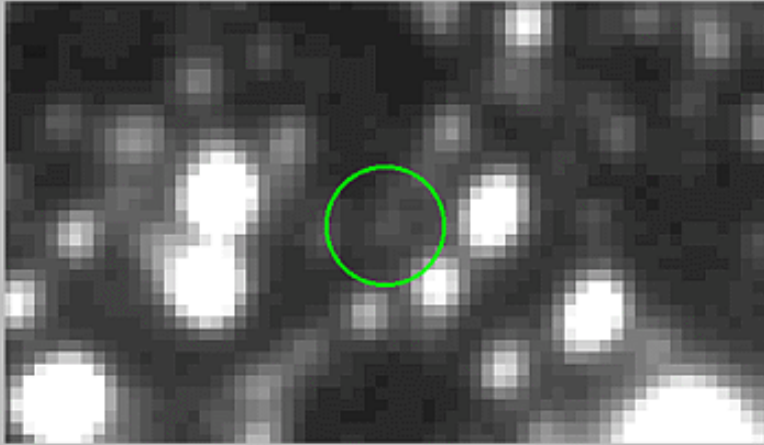
$$d = 1,120 \pm 0,007$$

$$M_p = 1,5^{+0,1}_{-1,2} M_J$$

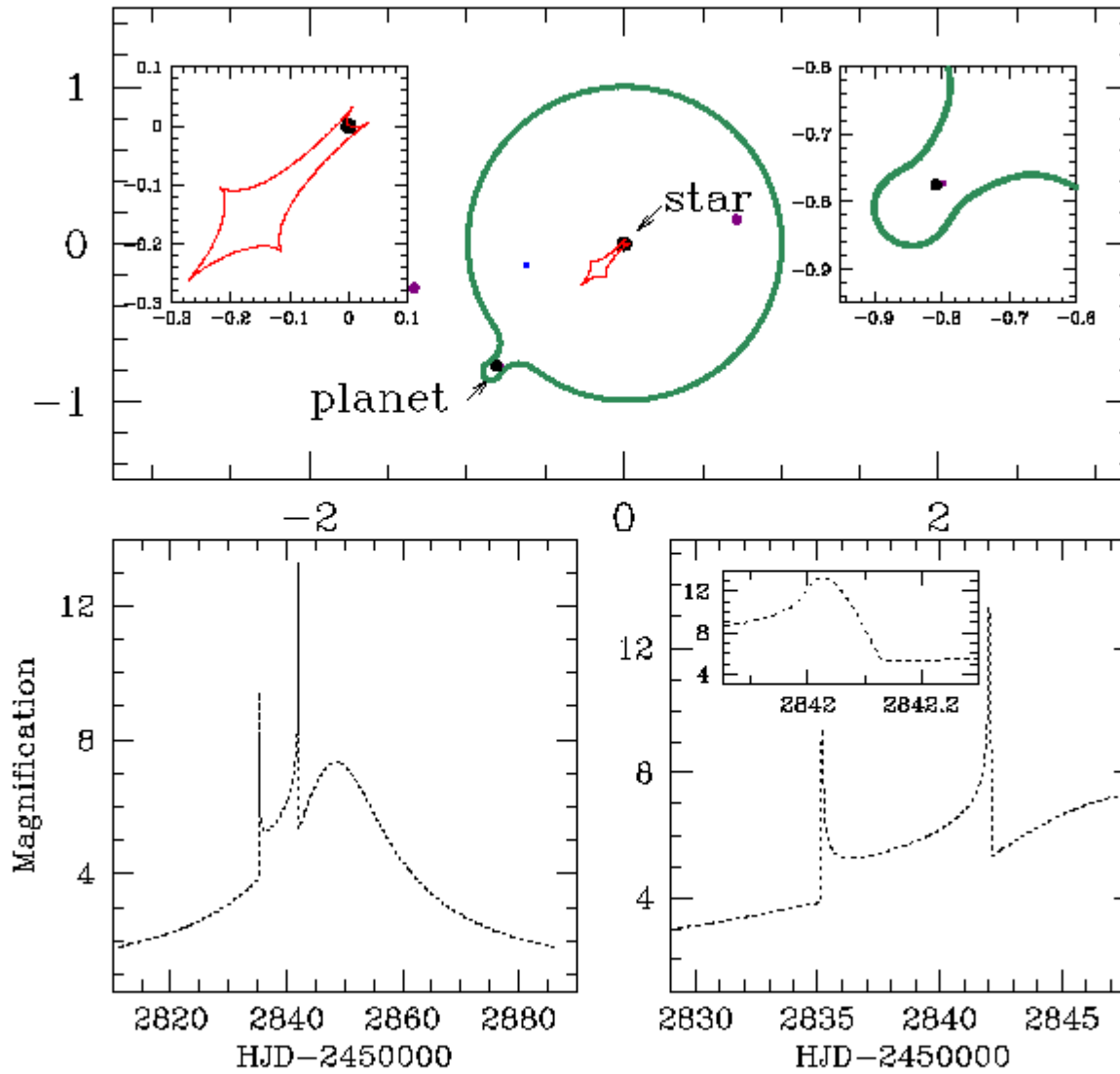
$$r_{\perp} = 3,0^{+0,1}_{-1,7} AU$$

$$M_* = 0,36^{+0,03}_{-0,28} M_{\odot}$$

# OGLE 2003-BLG-235 / MOA 2003-BLG-53



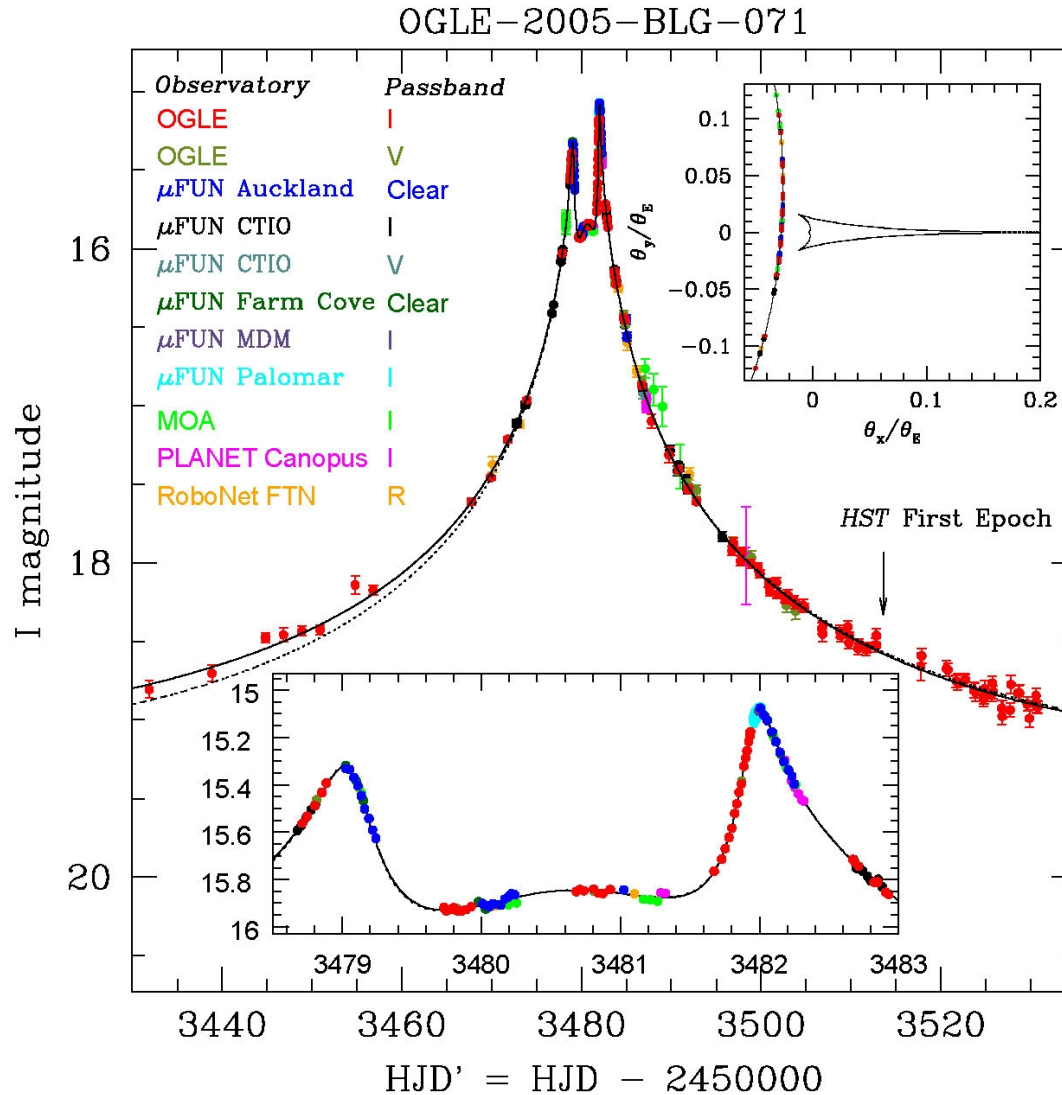
# OGLE 2003-BLG-235 / MOA 2003-BLG-53





# OGLE 2005-BLG-071

Udalski et al. (2005), Dong et al. (2009)



$$q = 0,0072^{+0,0004}_{-0,0002}$$

$$d = 1,285^{+0,008}_{-0,007}$$

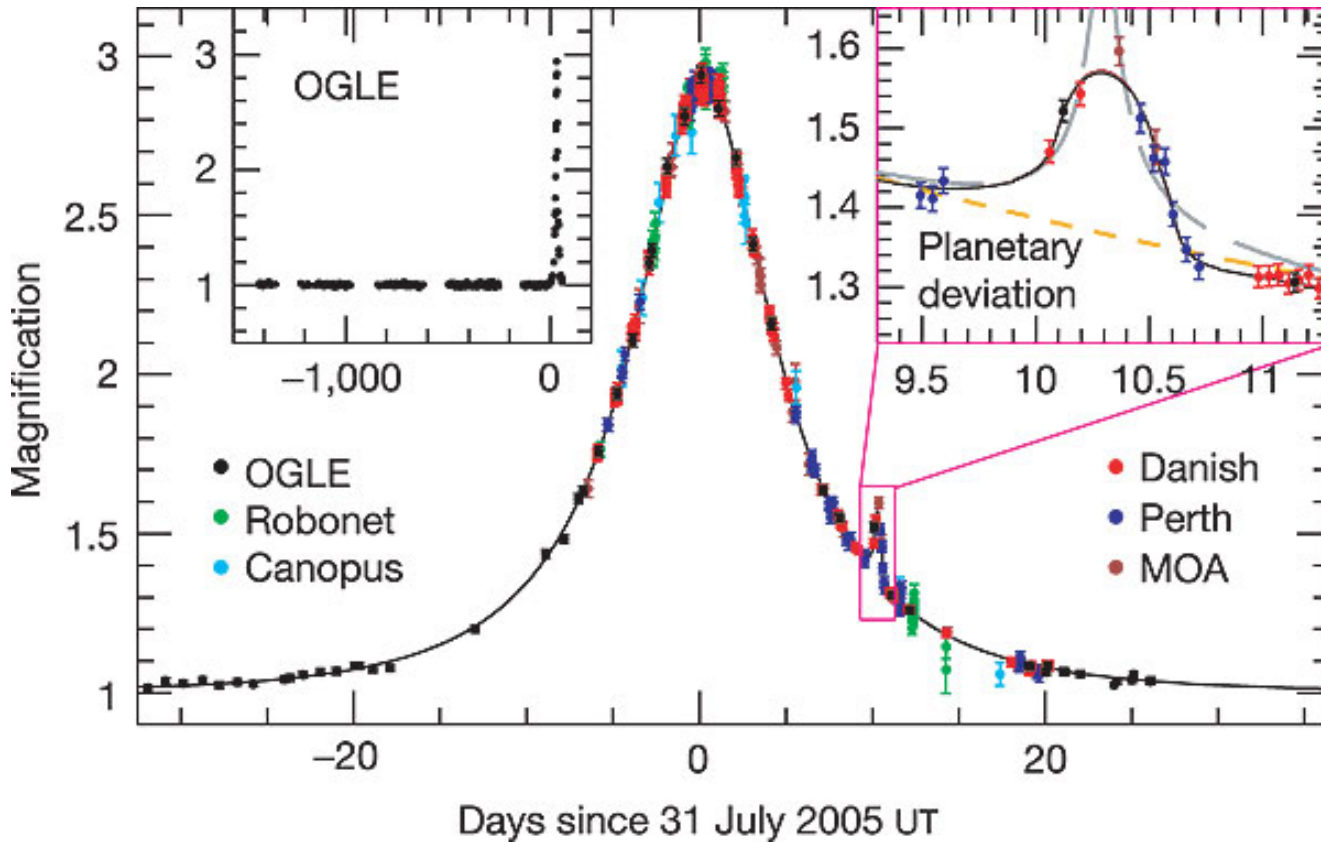
$$M_p = 3,5 \pm 0,3 M_J$$

$$r_{\perp} = 3,6 \pm 0,2 AU$$

$$M_* = 0,46 \pm 0,04 M_{\odot}$$

# OGLE 2005-BLG-390

Beaulieu et al. (2006)



$$q = 7,6 \pm 0,7 \times 10^{-5}$$

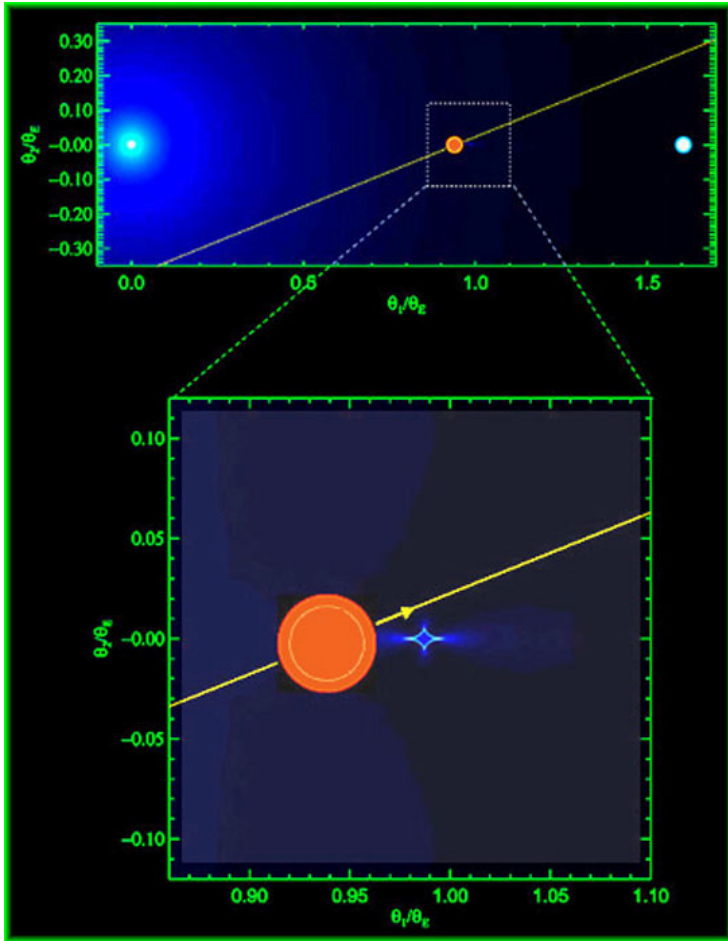
$$d = 1,610 \pm 0,008$$

$$M_P = 5,5^{+5,5}_{-2,7} M_{\oplus}$$

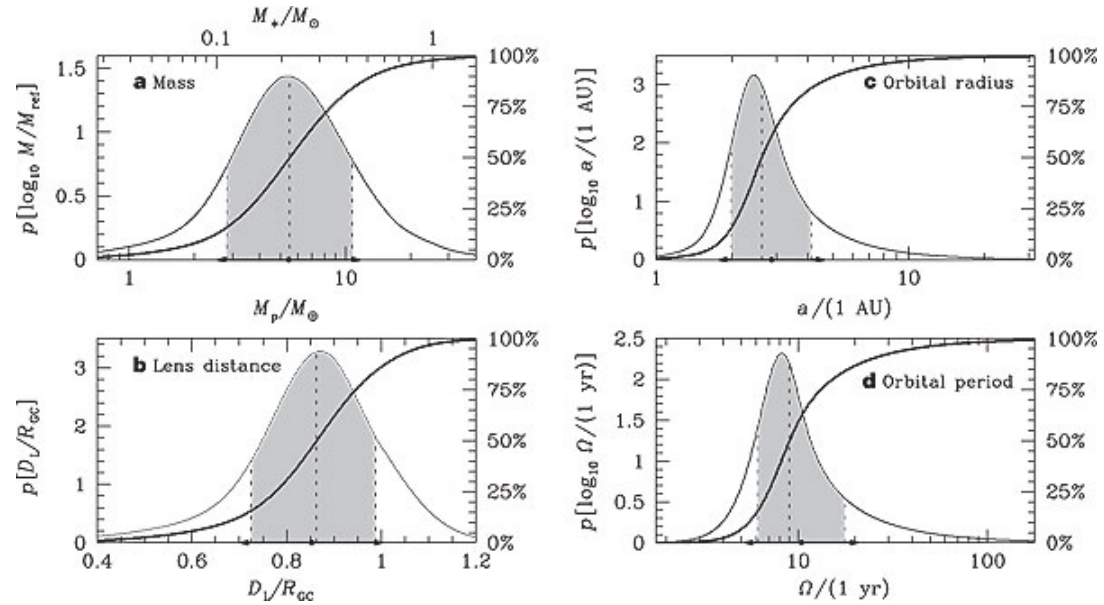
$$r_{\perp} = 2,6^{+1,5}_{-0,6} AU$$

$$M_* = 0,22^{+0,21}_{-0,11} M_{\odot}$$

# OGLE 2005-BLG-390

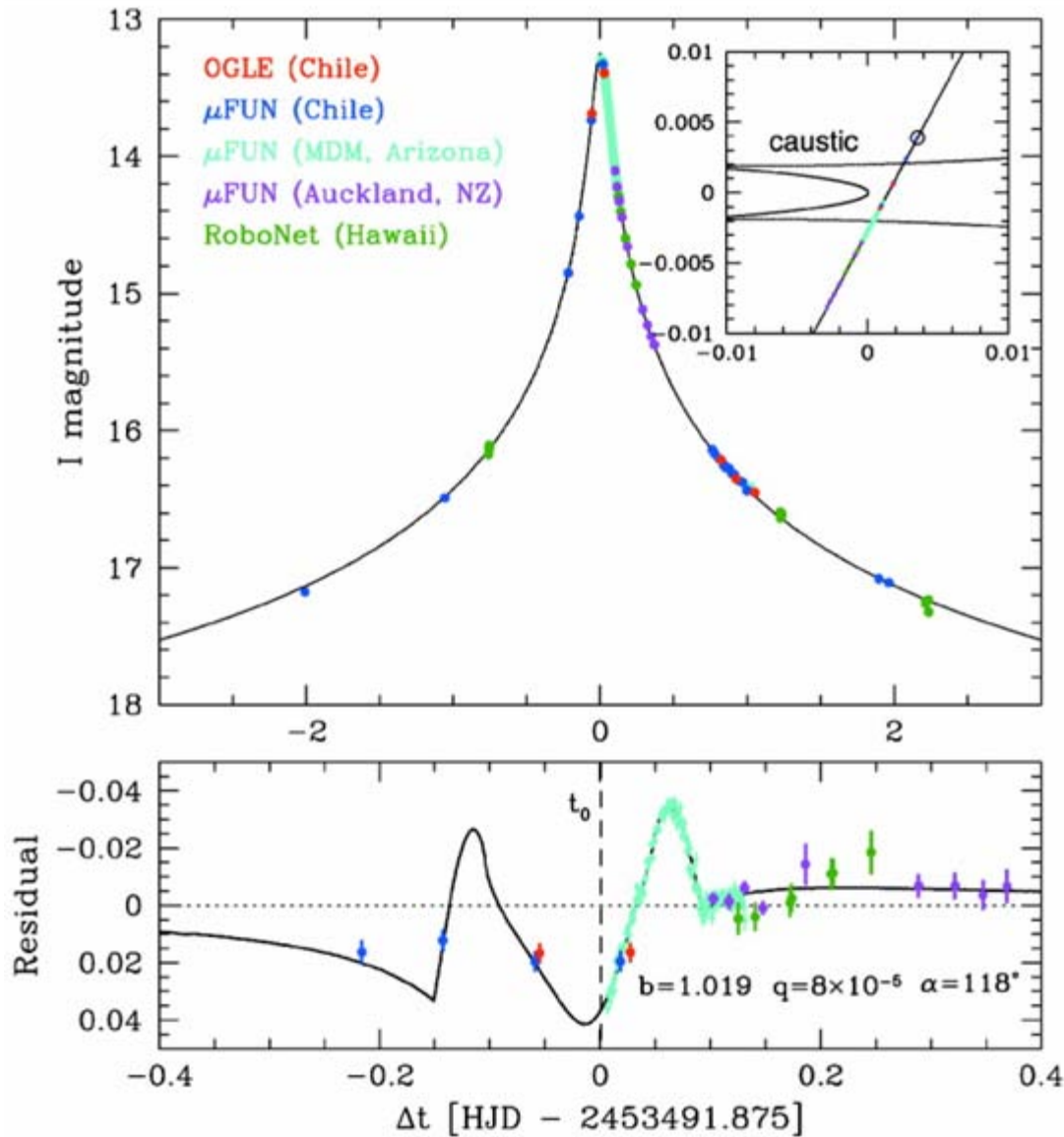


PLANET / D. Kubas



# OGLE 2005-BLG-169

Gould et al. (2006)



$$q = 8_{-3}^{+2} \times 10^{-5}$$

$$d = 1,00 \pm 0,02$$

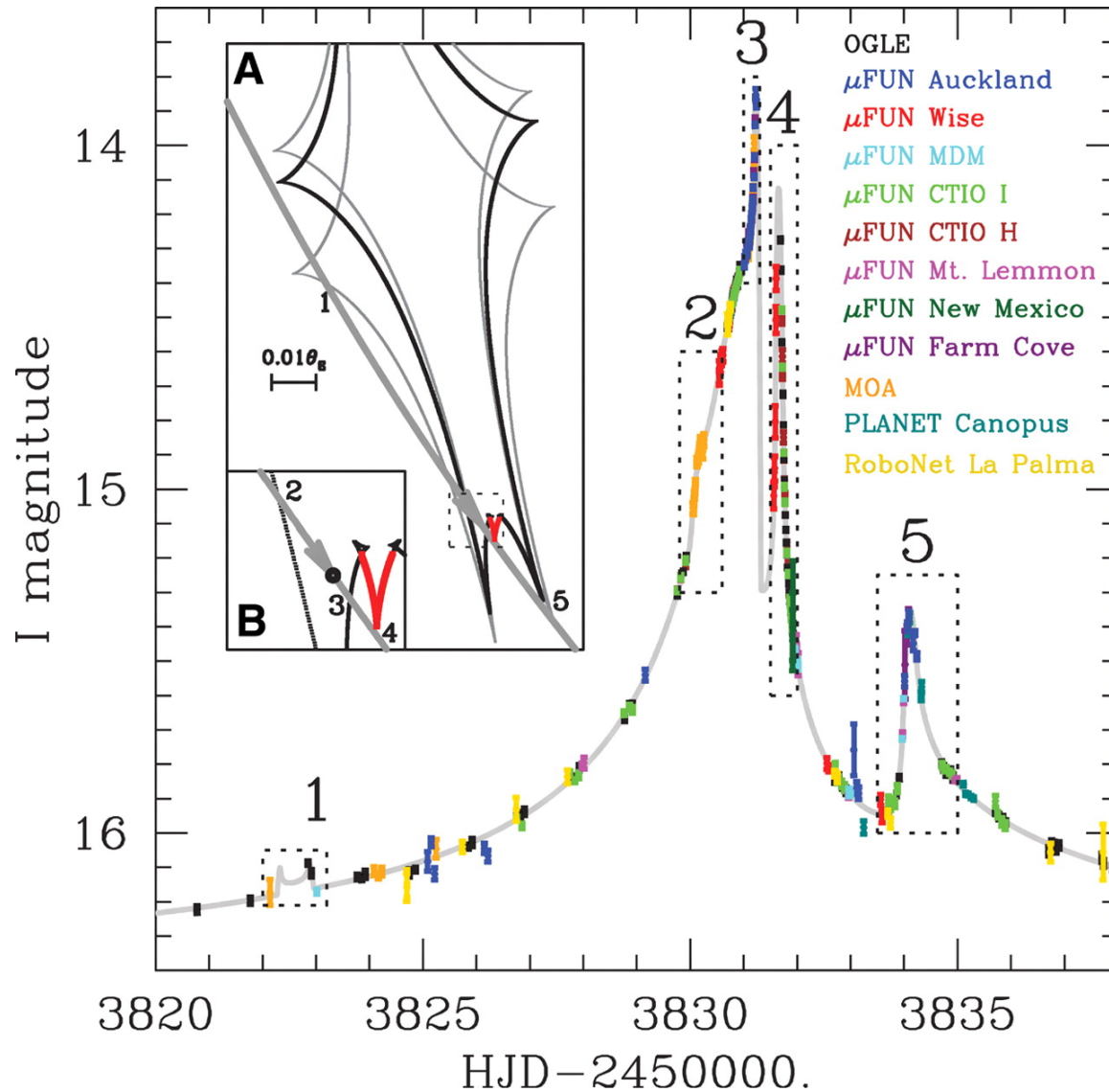
$$M_p = 13M_\oplus$$

$$r_\perp = 2,7AU$$

$$M_* = 0,49_{-0,29}^{+0,23} M_\odot$$

# OGLE 2006-BLG-109

Gaudi et al. (2008)



$$M_b = 0,71 \pm 0,08 M_J$$

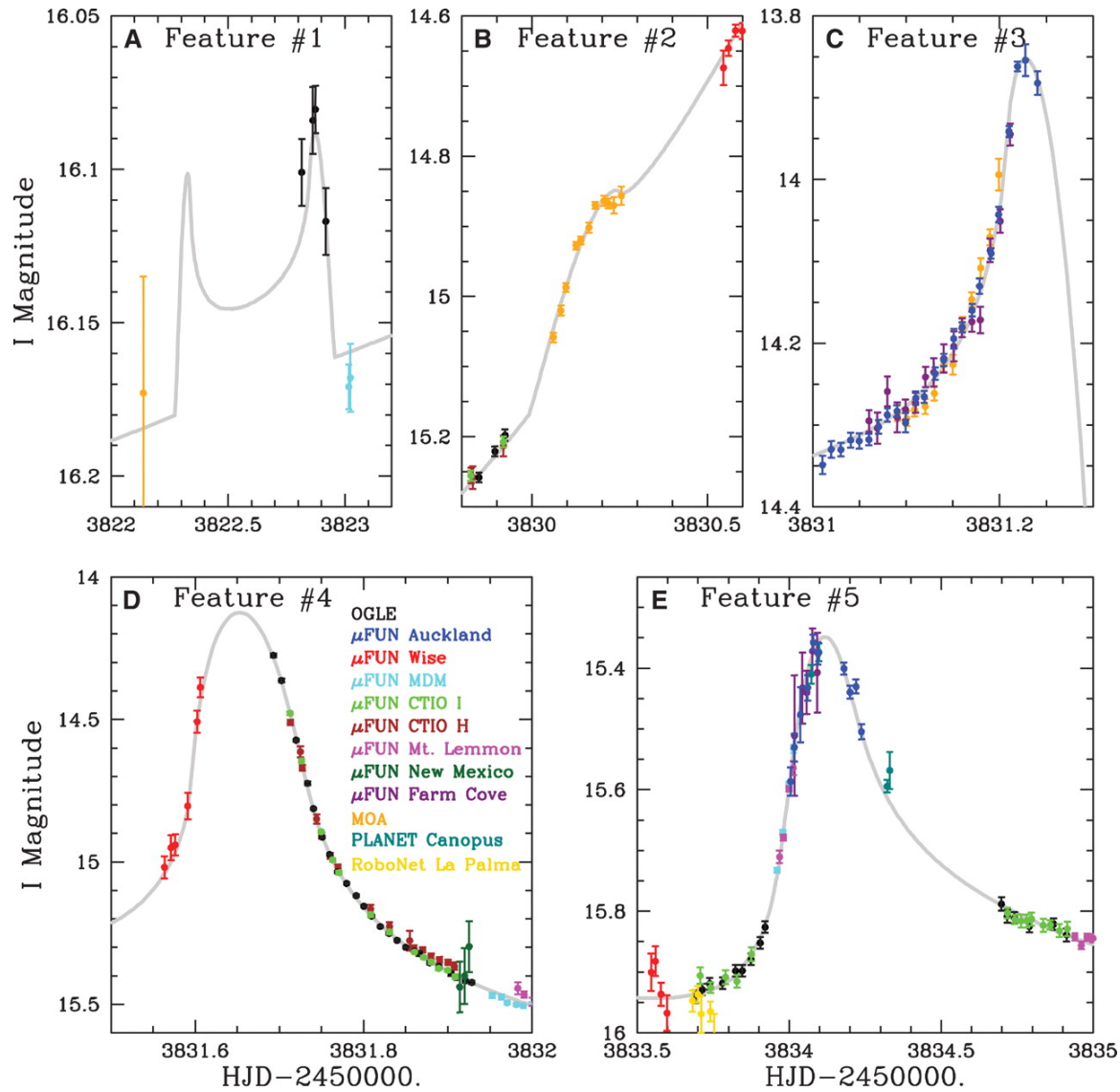
$$a_b = 2,3 \pm 0,2 AU$$

$$M_c = 0,27 \pm 0,03 M_J$$

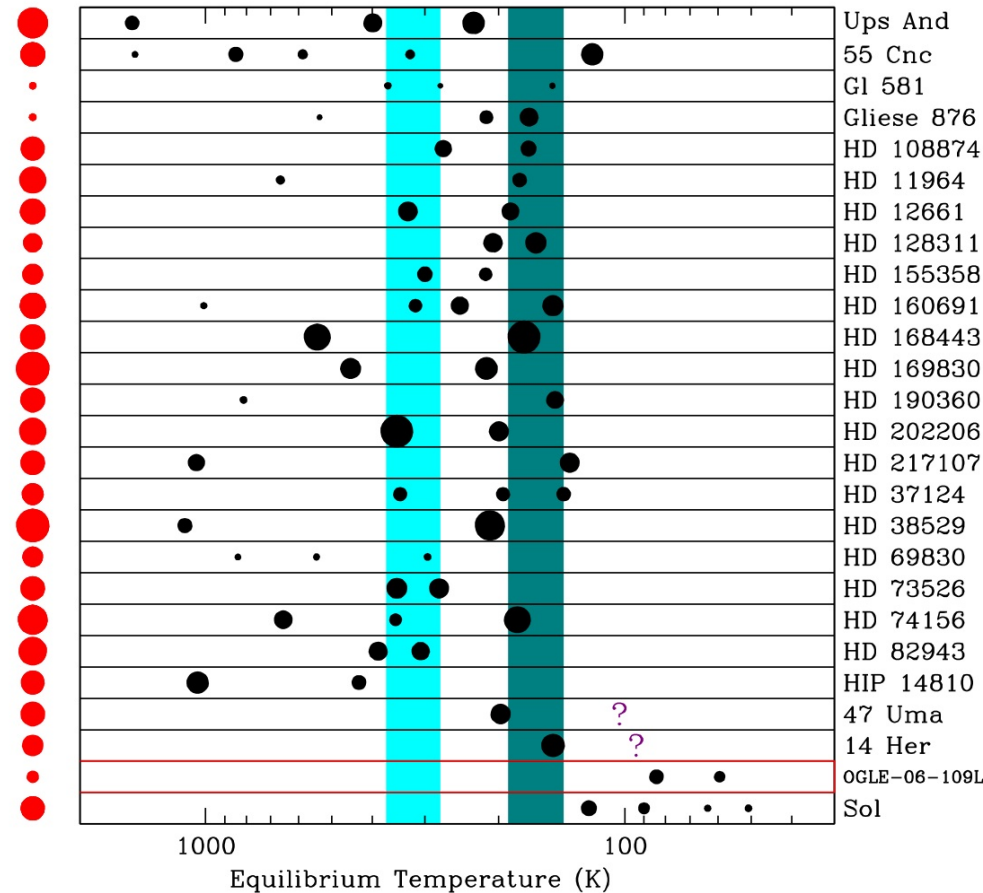
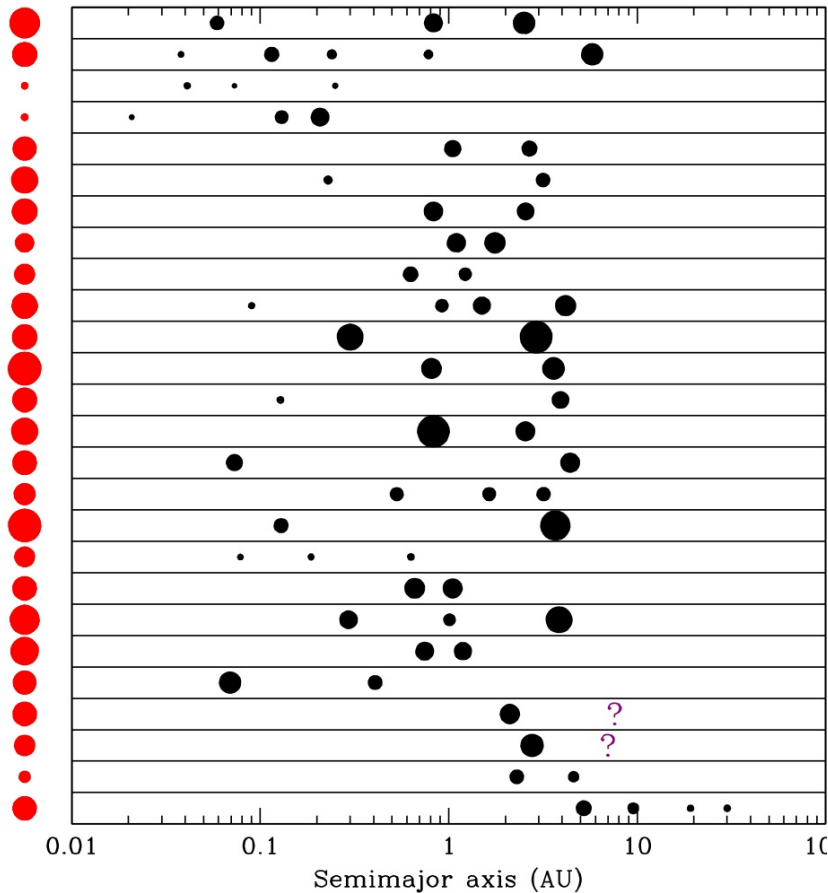
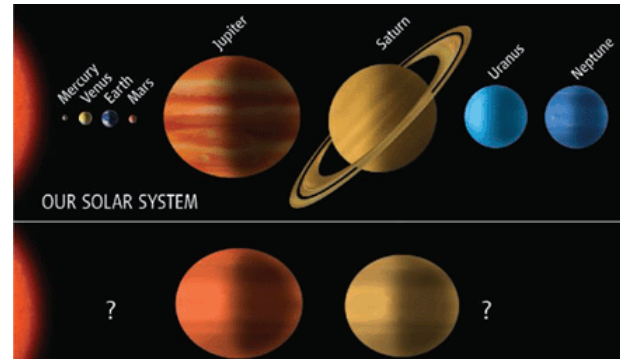
$$a_c = 4,6 \pm 0,5 AU$$

$$M_* = 0,50 \pm 0,05 M_\odot$$

# OGLE 2006-BLG-109

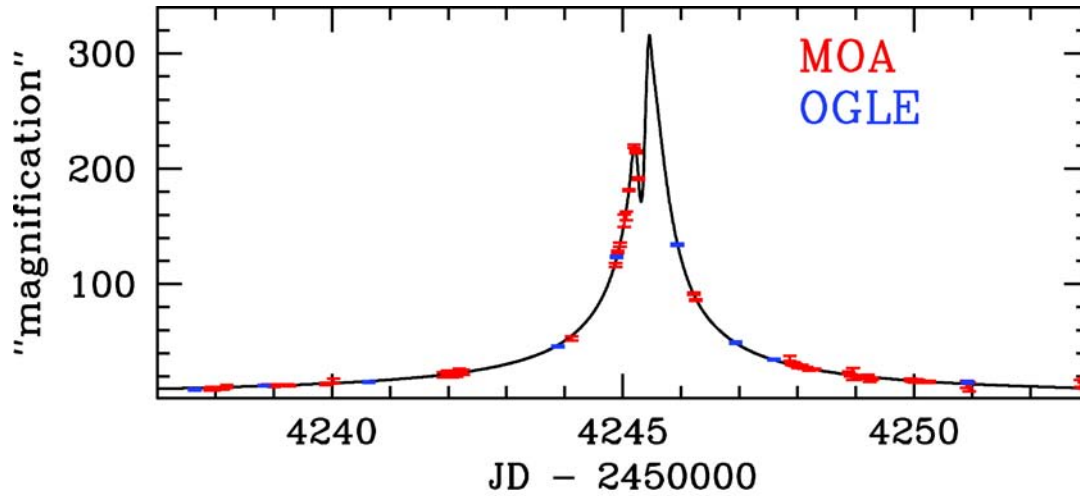


# OGLE 2006-BLG-109



# MOA 2007-BLG-192

Bennett et al. (2008)



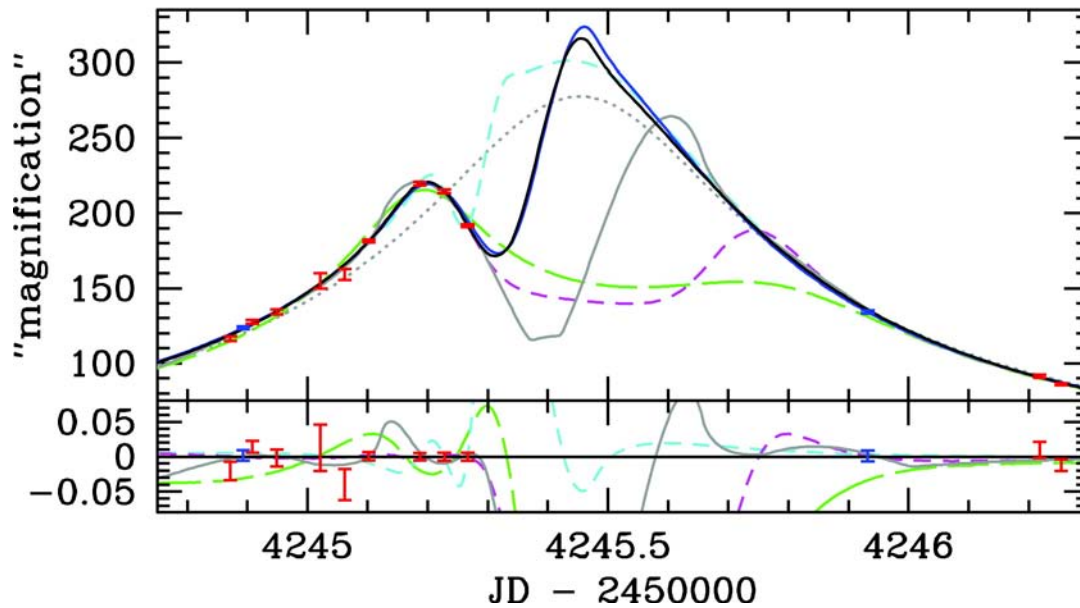
$$q = 1,2 \times 10^{-4}$$

$$d = 1,12$$

$$M_P = 3,3^{+4,9}_{-1,6} M_{\oplus}$$

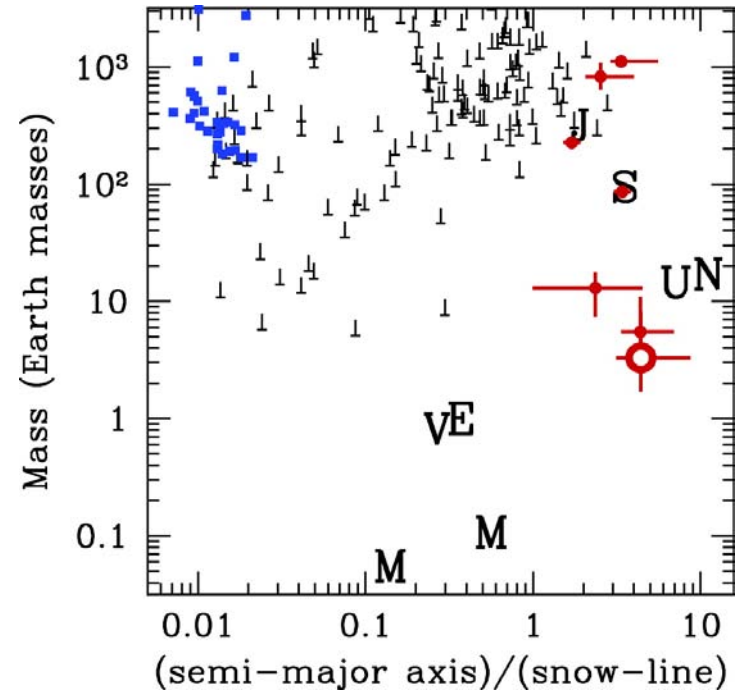
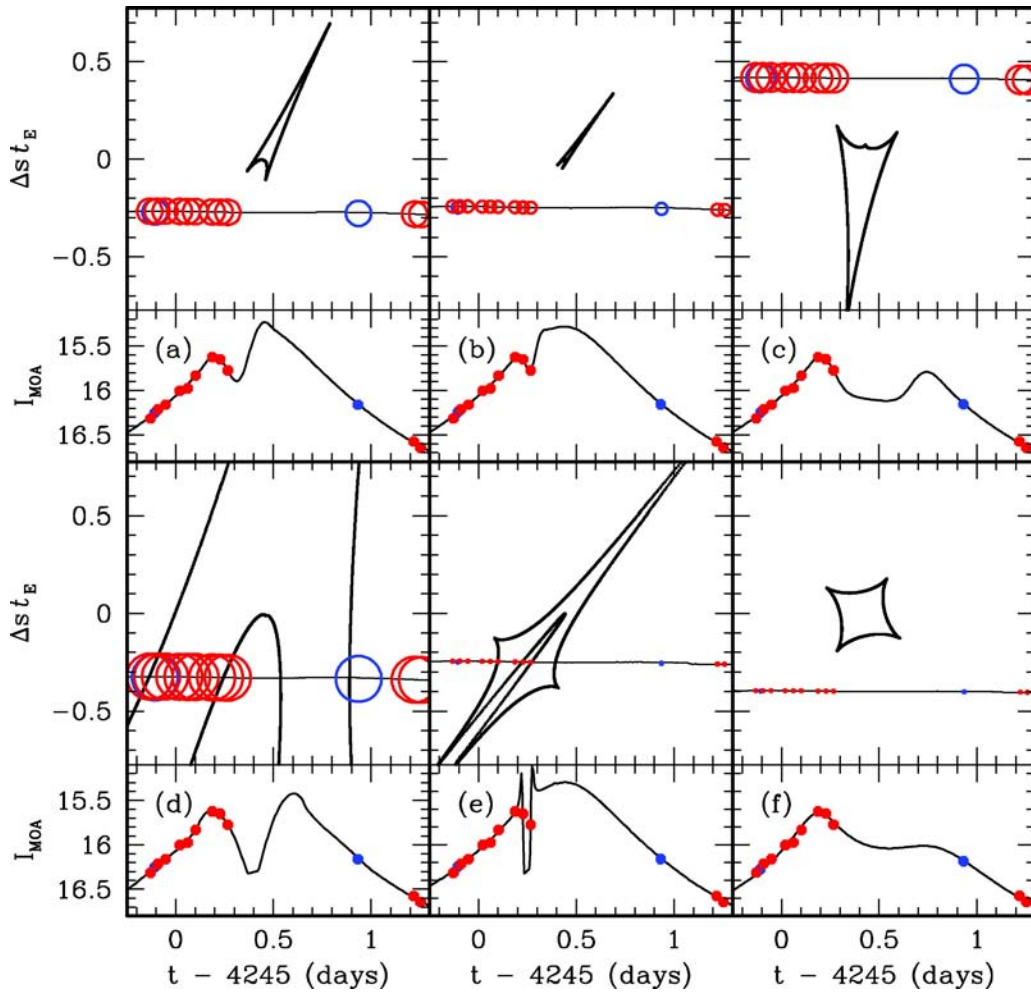
$$r_{\perp} = 0,62^{+0,22}_{-0,16} AU$$

$$M_* = 0,060^{+0,028}_{-0,021} M_{\odot}$$





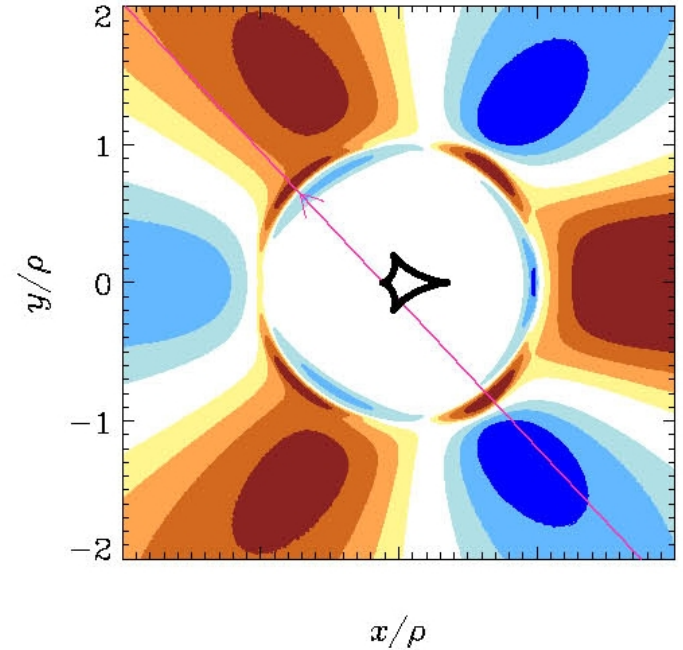
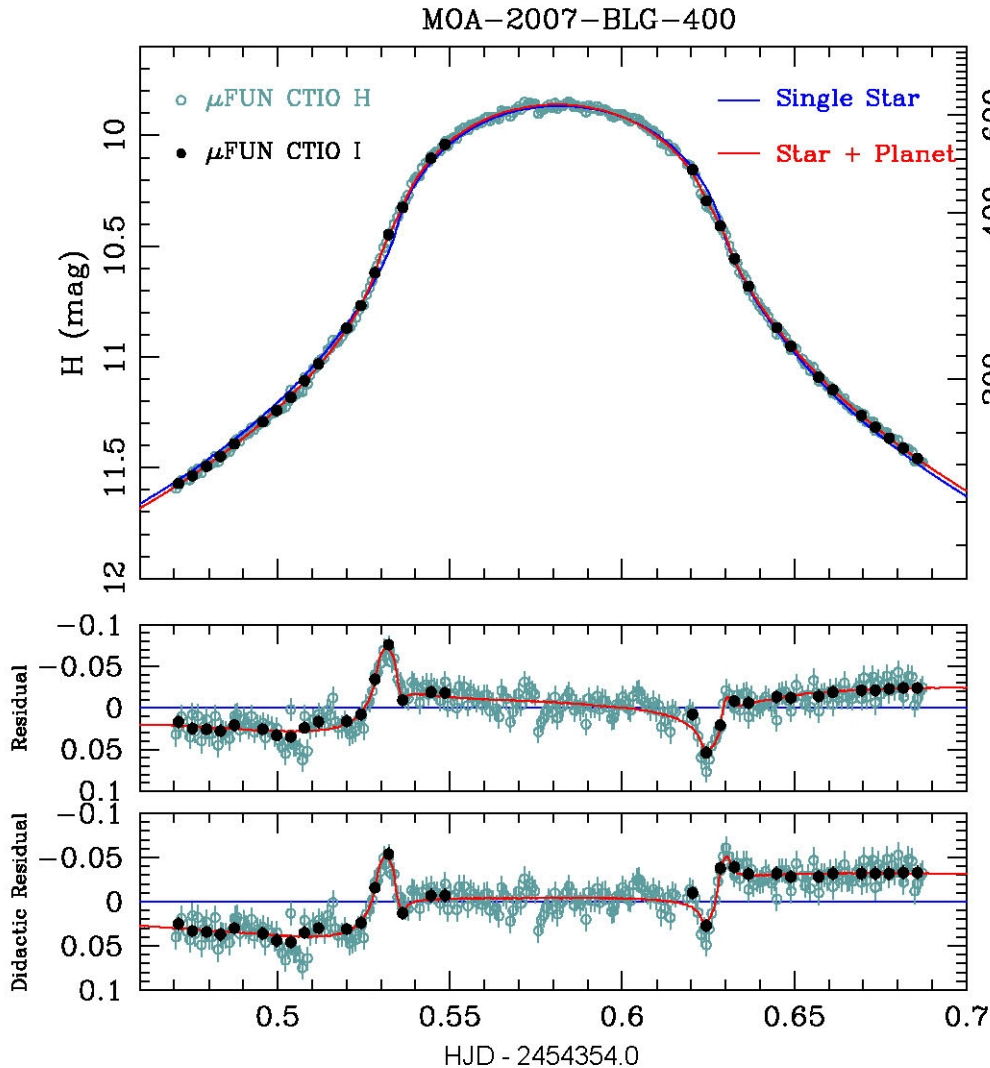
# MOA 2007-BLG-192



*D.P.Bennett (2008)*

# MOA 2007-BLG-400

Dong et al. (2009)



$$q = 0,0026 \pm 0,0004$$

$$d = 2,9 \pm 0,2$$

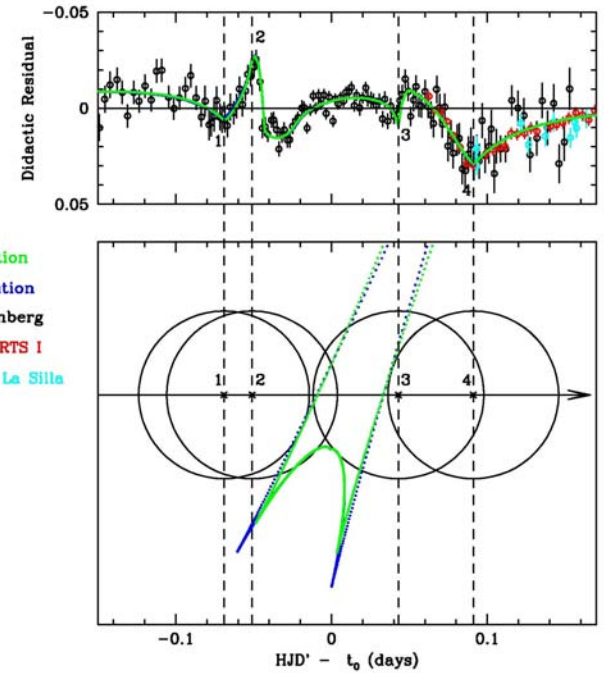
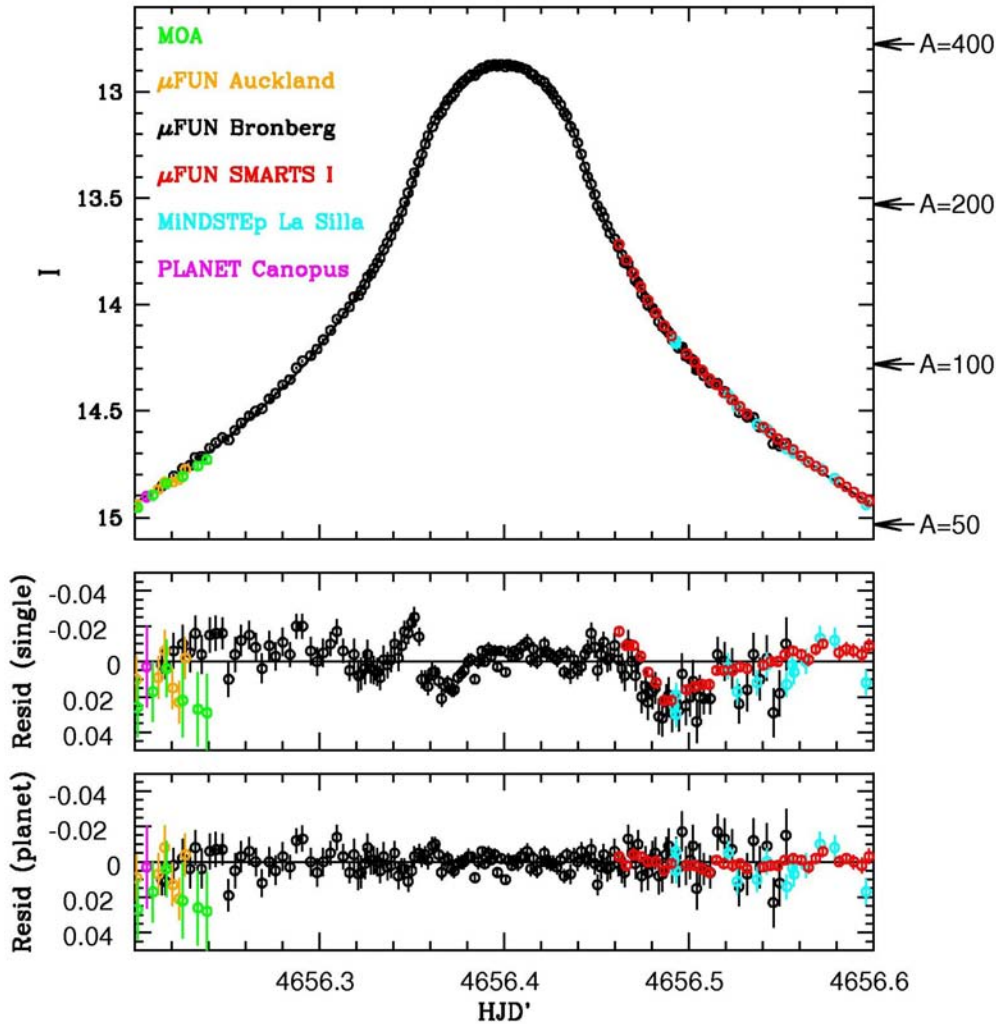
$$M_P = 0,82^{+0,52}_{-0,33} M_J$$

$$a = 6,5^{+3,2}_{-1,2} AU$$

$$M_* = 0,30^{+0,19}_{-0,12} M_O$$

# MOA 2008-BLG-310

Janczak et al. (2009)



$$q = (3,31 \pm 0,26) \times 10^{-4}$$

$$d = 1,085 \pm 0,003$$

$$M_P = 74 \pm 17 M_{\oplus}$$

$$r_{\perp} = 1,25 \pm 0,10 AU$$

$$M_* = 0,67 \pm 0,14 M_{\odot}$$

Exoplanets: 50+262+8+5=325 (Mar 2009)

